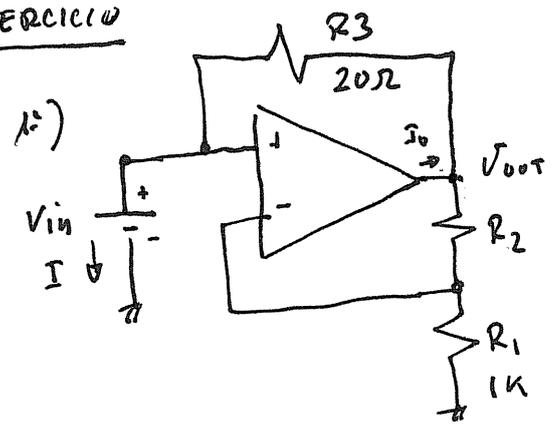


# RESOLUCIÓN CUESTIONES Y EJERCICIOS EXAMEN 8-2-99 DE ELECTRONICA ANALOGICA. (EXAMEN COMPLETO)

## EJERCICIO



$$|I_0|_{\text{MÁXIMO}} = 20 \mu\text{A}$$

$$|V_0|_{\text{MÁX}} = 15 \text{V}$$

Calculemos el valor de  $V_{out}$ ,  $I_0$  e  $I$  en el caso de que el funcionamiento del A.O. sea lineal:

La configuración es la de un A.O. no invertidor.  
Es inmedida en su funcionamiento lineal se cumple:

$$V_{out} = \left(1 + \frac{R_2}{R_1}\right) V_{in}$$

Nota:  $R_3$  no introduce realimentación si  $V_{in}$  es una fuente ideal.

$$I = \frac{V_{out} - V_{in}}{R_3} \quad \text{Expresión cierta siempre que } |I_0| < 20 \mu\text{A}$$

Aplicando nudos en  $V_{out}$ , podemos deducir el valor de  $I_0$

$$V_{out} (G_2 + G_3) - G_3 V_{in} - G_2 \cdot \frac{R_1}{R_1 + R_2} V_{out} - I_0 = 0$$

o lo que es lo mismo:

$$I_0 = \frac{V_{out} - V_{in}}{R_3} + \frac{V_{out}}{R_1 + R_2} = V_{out} \left[ \frac{1}{R_3} + \frac{1}{R_1 + R_2} \right] - \frac{V_{in}}{R_3}$$

$$I_0 = V_{out} \left[ \frac{1}{R_3} + \frac{1}{R_1 + R_2} \right] - \frac{V_{in}}{R_3}$$

Como  $R_1 = 1 \text{K}$  y  $R_3 = 20 \Omega$ , como se previó desde el principio

$$I_0 \approx \frac{V_{out} - V_{in}}{R_3} \approx I, \text{ ya que la corriente}$$

através del divisor de división  $R_2$  y  $R_1$  es despreciable frente a la que circula por  $R_3$

A)  $R_2 = 1K\Omega \Rightarrow V_{out} = 2 V_{in}$   $I_0 = \frac{V_{out} - V_{in}}{20} = I$

$V_{in} = 0 \Rightarrow V_{out} = 0$   $I = 0$

$V_{in} = 1,5V \Rightarrow V_{out} = 3V$   $I = \frac{3 - 1,5}{20} = 75mA$

$V_{in} = 6$   $V_{out} = 12V$   $I = \frac{12 - 1,5}{20} = 525mA \rightarrow$  Protección  $\Rightarrow I = 200mA$

$V_{in} = 12V$   $V_{out} = 24V \Rightarrow$  saturación  $\Rightarrow V_{out} = 15V \Rightarrow I = \frac{15 - 12}{20} = 150mA$

B)  $R_2 = 500\Omega \Rightarrow V_{out} = 1,5 V_{in}$   $I_0 = \frac{V_{out} - V_{in}}{20}$

$V_{in} = 0$   $V_{out} = 0$   $I = 0$

$V_{in} = 1,5V$   $V_{out} = 2,25V$   $I = 37,5mA$

$V_{in} = 6V$   $V_{out} = 9V$   $I = \frac{9 - 6}{20} = 150mA$

$V_{in} = 12V$   $V_{out} = 18 \Rightarrow$  SAT.  $\Rightarrow V_{out} = +15 \Rightarrow I = \frac{15 - 12}{20} = 150mA$

C)  $R_2 = 200\Omega \Rightarrow V_{out} = 1,2 V_{in}$   $I = \frac{V_{out} - V_{in}}{20}$

$V_{in} = 0$   $V_{out} = 0$   $I = 0$

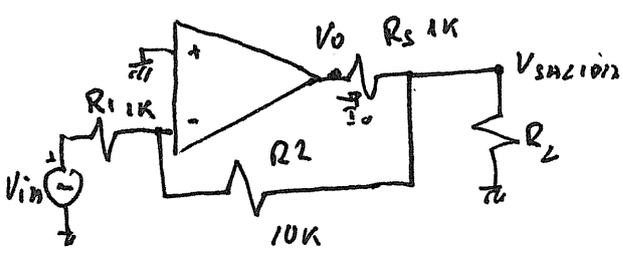
$V_{in} = 1,5V$   $V_{out} = 1,8V$   $I = 15mA$

$V_{in} = 6V$   $V_{out} = 7,2V$   $I = 60mA$

$V_{in} = 12V$   $V_{out} = 14,4V$   $I = \frac{14,4 - 12}{20} = 120mA$

2º EJERCICIO

Siempre y cuando el A.O. sea ideal ( $A_d \rightarrow \infty$ )  
 y  $V_0$  no alcance las tensiones de saturación y lo  
 la corriente  $I_0 < I_{MAX}$  :



$$V_{SAT(10)} = - \frac{R_2}{R_1} V_{in}$$

$$V_{SAT(10)} (G_s + G_L + G_2) - G_s V_0 - G_L \cdot 0 - G_2 V^- = 0$$

Si se cumplen las condiciones de linealidad  $V^+ = 0 \Rightarrow V^- = 0$

$$V_{SAT(10)} (G_s + G_L + G_2) - G_s \cdot V_0 = 0$$

$$V_0 = \frac{G_s + G_L + G_2}{G_s} V_{SAT(10)} = - \left( 1 + \frac{R_s}{R_2} + \frac{R_s}{R_2} \right) \cdot \frac{R_2}{R_1} V_{in}$$

$V_0 =$  ~~...~~ Como  $\frac{R_2}{R_1} = 10$

$$V_0 = -10 \left[ 1 + \frac{R_s}{R_2} + \frac{R_s}{R_2} \right] V_{in}$$

La anterior expresión es cierta en tanto  $|V_0| < V_{SAT}$   $|V_0| < 15V$

y  $|I_0|$  no supere los 25mA.

donde:  $I_0 = \frac{V_0 - V_{SAT}}{1K}$

$V_{SAT} = -10V_{in} = -10V$

$V_0 = -21V_{in}$

$I = \frac{V_0 - V_{SAT}}{R_S} = \frac{-21V_{in} + 10V_{in}}{R_S} = \frac{-11}{1K} V_{in}$

A)  $R_L = 1K$

$\Rightarrow$

$V_{in} = 100mV \Rightarrow V_0 = -10 \left[ 1 + \frac{R_S}{R_L} + \frac{1}{10} \right] V_{in} = -10 \left[ 1 + 1 + \frac{1}{10} \right] 0.1 = -2.1V$

$V_{in} = 300mV \Rightarrow$

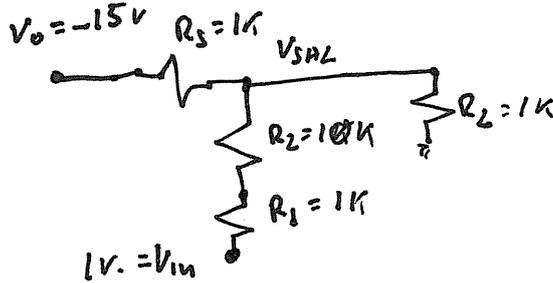
$V_0 = -2.1 \cdot 0.3 = -0.63V$   $I_0 = \frac{-0.63 + 3}{1K} = -3.3mA$

$V_{SAT} = -10V_{in} = -3V$

$V_{in} = 1V \Rightarrow$

$V_0 = -21 \cdot 1 = -21V \Rightarrow SAT$

CIRCUITO EQUIVALENTE



$V_{SAT} \cdot \left[ \frac{1}{1K} + \frac{1}{11K} + \frac{1}{1K} \right] - \left( \frac{1}{1K} \cdot (-15) \right) - \frac{1}{11K} \cdot 1 = 0$

$V_{SAT} [2.091] = -15$   
 $V_{SAT} = -\frac{15}{2.091} = -7.174V$

$|I_0| = \left| \frac{-15 + 7.174}{1K} \right| < I_{MAX}$

B)  $R_L = 500\Omega$

Siempre que se cumple la hipótesis de funcionamiento lineal:

$V_{SAT} = -10V_{in}$   
 $V_0 = -31V_{in}$   
 $I_0 = (V_0 - V_{SAT}) / 1K$

y con  $R_L = 500\Omega$ :  $V_0 = -10 \left[ 1 + \frac{1000}{500} + 0.1 \right] V_{in}$

$V_0 = -10 [3.1] V_{in} = -31V_{in}$

$V_{in} = 100mV$   $V_0 = -31 \cdot 0.1 = -3.1V \Rightarrow V_{SAT} = -1V$   $|V_0| < 25mV$

$V_{in} = 300mV$   $V_0 = -31 \cdot 0.3 = -9.3V \Rightarrow V_{SAT} = -3V$   $|V_0| < 25mV$

$V_{in} = 1V$   $V_0 = -31 \cdot 1 = -31V \Rightarrow SATURACION$

para a ser el mismo del caso anterior pero con  $R_L = 500\Omega = 0.5K$ .

$V_{SAT} \left[ \frac{1}{1K} + \frac{1}{11K} + \frac{1}{0.5K} \right] - \left( -15 \cdot \frac{1}{1K} \right) - \frac{1}{11K} = 0$

$V_{SAT} = \frac{-15}{3.091} = -4.85V$   $|I_0| < 25mA$

$R_L = 100 \Omega$

$V_{SA21012} = -10 V_{in}$

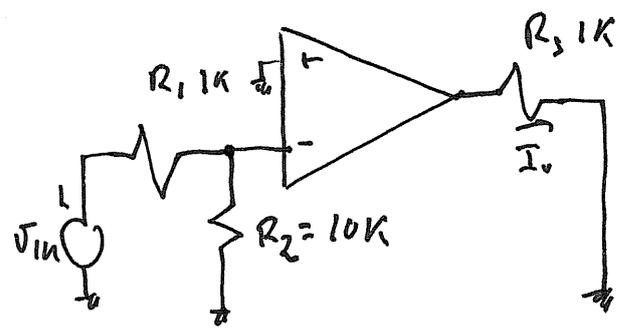
$V_0 = -10 \left[ 1 + \frac{1k}{0.1k} + \frac{1}{10} \right] V_{in} = -10 \left[ 1 + 10 + \frac{1}{10} \right] V_{in} = -10 \times 11.1 V_{in}$

$V_0 = -111 V_{in}$  *car.*

$111 V_{in} < 15 \Rightarrow V_{in} < \frac{15}{111} = 0.135 V$

$V_{in \text{ maximum}} = \underline{\underline{135 mV}}$

$R_L = 0$  .  $\hat{I}$  CIRCUITU ECGUIVACENTE  $\Rightarrow$  ATILUR:



Nu există reclamen<sup>ta</sup>cia.

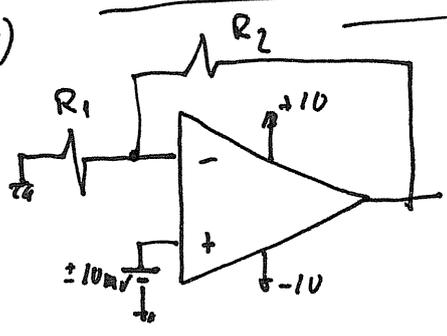
cu  $V_{in} = +1V \Rightarrow V^- > 0$

cu  $V^+ = 0 \Rightarrow$

$V^- > V^+ \Rightarrow V_0 = -15V$

$I_0 = -15 mA$

20)



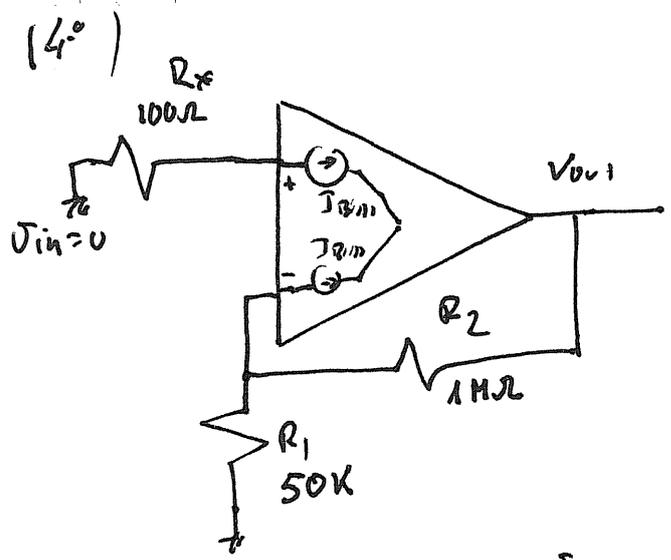
$V^- (G_1 + G_2) - G_1 = 0 - G_2 = V_0 = 0$

$V^- = V^+ \Rightarrow V^- = \pm 10 mV$

$\pm 10 mV (G_1 + G_2) = G_2 V_0$

$V_0 = \pm 10 mV \left[ 1 + \frac{G_1}{G_2} \right] = \pm 10 mV \left[ 1 + \frac{R_2}{R_1} \right]$

$V_0 = \pm 10 mV \cdot [1 + 200] = 201 \cdot 10 mV = \underline{\underline{2.01 V}}$



En ausencia de señal, ( $V_{in} = 0$ ) si el A.O. está funcionando linealmente  $V^+ = V^-$

$$V^+ = 0 - R_x I_{B1} = -R_x I_{B1}$$

En el nudo G:

$$V^- (G_1 + G_2) - G_2 V_{out} + I_{B2} = 0$$

$$V_{out} = I_{B2} \cdot R_2 + V^- \left[ \frac{G_1 + G_2}{G_2} \right]$$

$$V_{out} = R_2 I_{B2} + \left( 1 + \frac{R_2}{R_1} \right) V^- = R_2 I_{B2} + A \cdot V^-$$

$$V_{out} = R_2 I_{B2} + A(-R_x I_{B1})$$

$$V_{out} = [R_2 - A R_x] I_{B2}$$

- $R_2 = 1M\Omega$
- $R_x = 100k$
- $A = 21$

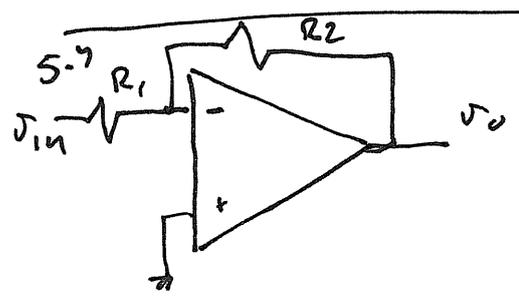
$$V_{out} = [1M\Omega - 21 \cdot 100k] \cdot 1\mu A$$

$$V_{out} = [1M\Omega - 2.1k] \cdot 1\mu A \approx \underline{\underline{1V}}$$

Si deseamos que  $V_{out} \approx 0 \Rightarrow$

$$R_2 = A R_x \Rightarrow R_x = \frac{R_2}{A} = \frac{1M\Omega}{21} = \underline{\underline{47.6k}}$$

$R_x = 47.6k \Rightarrow$  Resistencia adicional  $47.6k - 100k \approx \underline{\underline{47.5k}}$



$$V_o = - \frac{100k}{2k} V_{in} = - \frac{R_2}{R_1} V_{in} = -50 V_{in}$$

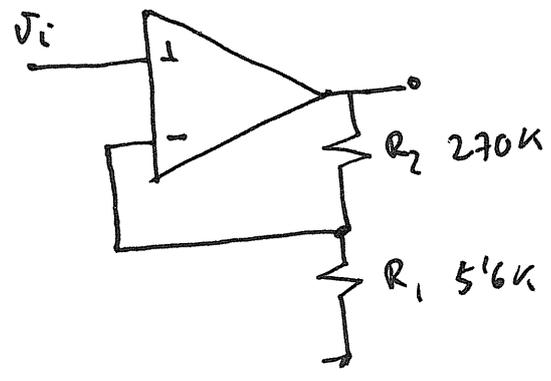
$$V_{in} = (10mV) \cdot \sin \omega t$$

$$V_{out} = -0.5V \cdot \sin \omega t$$

$$\left. \frac{dV}{dt} \right|_{max} |_{t=0} = 0.5 \cdot \omega = 0.5 \cdot 2\pi \cdot f \leq 1V/\mu s$$

$$f < \frac{10^6}{0.5 \cdot 2\pi} = 318.3kHz$$

6.2)



$$A_d(j\omega) = \frac{A_{dc}}{1 + j \frac{\omega}{\omega_B}}$$

$$A_{d0} = \left(1 + \frac{R_2}{R_1}\right) = 49.21$$

GANANCIA = ANCHURA DE BANDA =  $c_b = A_{d0} \omega_{c_b}$  = anchura banda crítica

$$= 2 \times 10^4 \times 12 = 24 \times 10^4$$

$$24 \times 10^4 = 49.21 \omega_B \Rightarrow \omega_B = \frac{24 \times 10^4}{49.21} \approx 4.8777 \text{ Hz}$$

7.2)

$$I_d = I_s \left( e^{\frac{V_d}{V_T}} - 1 \right) = 10^{-15} \left[ e^{\frac{V_d}{25 \text{ mV}}} - 1 \right]$$

$$\uparrow \quad \quad \quad 3 \text{ mA} \approx 10^{-3} \quad e^{\frac{V_d}{25 \text{ mV}}}$$

$$\frac{V_d}{25 \text{ mV}} = \ln \frac{3 \times 10^{-3}}{10^{-15}} = 27.73$$

$$V_d = 25 \text{ mV} \times 27.73 = \underline{\underline{0.717 \text{ V}}}$$

8.2)

$$I_s(T) = I_s(T_R) \cdot 2^{\frac{T-T_R}{5}}$$

a  $T = 0^\circ\text{C} (273^\circ\text{K}) \quad I_s(273^\circ\text{K}) = I_s(27^\circ\text{C}) \cdot 2^{\frac{(273-300)}{5}}$

$$I_s(0^\circ\text{C}) = 10^{-15} \cdot ( ) = 2.1567 \times 10^{-17}$$

$$V_d = \frac{3 \times 10^{-3}}{2.1567 \times 10^{-17}} \cdot V_T(0^\circ\text{C})$$

$$V_d = \frac{V_T(27^\circ\text{C}) - 25 \text{ mV}}{2.73} \cdot x \quad \Rightarrow \quad x = \frac{273}{300} \cdot 25 \text{ mV} = 22.75 \text{ mV}$$

$$V_d(0^\circ\text{C}) = \underline{\underline{0.733 \text{ V}}}$$

$$I_S(100^\circ\text{C}) = 10^{-15} \cdot 2^{\frac{373-300}{5}} = 2.473 \times 10^{-11}$$

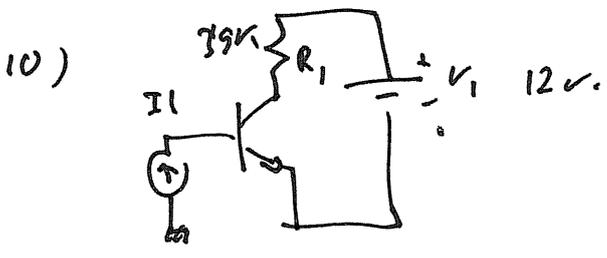
$$V_T(100^\circ\text{C}) = 25\text{mV} \cdot \frac{373}{300} = 31.1\text{mV}$$

$$C_D = 2.473 \times 10^{-11} \cdot e^{V_{d1}/V_T} \approx 3\text{mH}$$

$$V_{d1} = 31.1\text{mV} = \ln \frac{3 \times 10^{-3}}{2.473 \times 10^{-11}}$$

$$V_{d1} = 578.8\text{mV}$$

9) 
$$r_d = \frac{V_T}{I_{DQ}} = \frac{25\text{mV}}{3\text{mA}} = 8.33\Omega$$



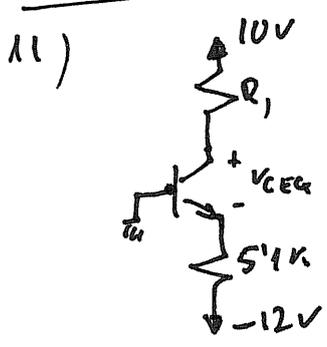
$$I_{CQ} = \beta F \cdot I_1 = 50 \cdot 20\mu\text{A} = 1\text{mA}$$

$$V_{CEQ} = 12 - 3.9\text{k} \cdot 1\text{mA} = 8.1\text{V}$$

$$0.2 = 12 - 3.9\text{k} \cdot I_{CMAX} \Rightarrow$$

$$I_{CMAX} = \frac{12 - 0.2}{3.9\text{k}} = 3.0256\text{mA} \Rightarrow$$

$$I_{BMAX} = 60.5\mu\text{A}$$



$$V_{CEQ} \approx 22 - (R_1 + 5.1\text{k}) I_{CQ}$$

$$\text{PR10 } I_{CQ} \approx \frac{-0.7 + 12}{5.1\text{k}} \approx 2.2\text{mA}$$

$$V_{CEQ} = 22 - (R_1 + 5.1\text{k}) \cdot 2.2\text{mA} = 5 \quad (2.24\text{mA})$$

$$17 = 2.2(R_1 + 5.1\text{k}) \Rightarrow$$

$$R_1 + 5.1\text{k} = 7.73\text{k}$$

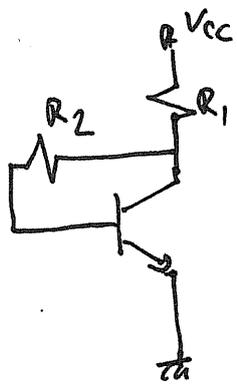
$$R_1 \approx 2.63\text{k}$$

$$\text{max } V_{BEQ} = 0.7\text{V}$$

$$R_1 = 2.49\text{k}$$

$$\text{max } V_{BEQ} = 0.6\text{V}$$

12).



$$E_{BE} = V_{CC}$$

$$E_{CE} = V_{CC}$$

$$R_B + R_E = R_1 + R_2$$

$$R_C + R_E = R_1$$

$$R_B + R_C = R_2$$

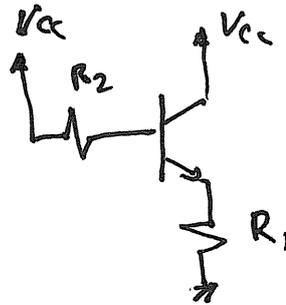
(7)

$$R_B = \frac{1}{2} [(R_B + R_E) + (R_C + R_E) - (R_C + R_E)] = \frac{1}{2} [R_1 + R_2 + R_2 - R_1]$$

$$R_C = \frac{1}{2} [(R_B + R_C) + (R_C + R_E) - (R_B + R_E)] = \frac{1}{2} [R_2 + R_1 - R_2 - R_1] = 0$$

$$R_E = \frac{1}{2} [(R_B + R_E) + (R_C + R_E) - (R_B + R_C)] = \frac{1}{2} [R_1 + R_2 + R_1 - R_2] = R_1$$

$R_B = R_2 = 100k$ $R_C = 0$ $R_E = R_1$
--



$$R_B + R_E = R_1 + R_2 = 101k\Omega$$

$$R_C + R_E = R_1 = 1k\Omega$$

$$R_B + R_C = R_2 = 100k$$

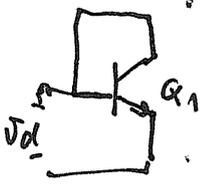
13)

$$I_{C\alpha} = \frac{E_{BE} - V_{BEQ}}{\frac{R_B}{\beta} + R_E(1 + \frac{1}{\beta})} = \frac{10 - 0.7}{\frac{100k}{\beta} + 1k(1 + \frac{1}{\beta})}$$

$$I_{C\alpha} \beta \rightarrow \infty = \frac{10 - 0.7}{1k} = 9.3mA$$

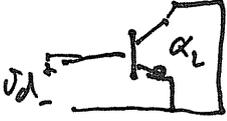
$$I_{C\alpha} \beta = 100 = \frac{100 - 0.7}{1k + 1k} \approx 4.65mA$$

14)



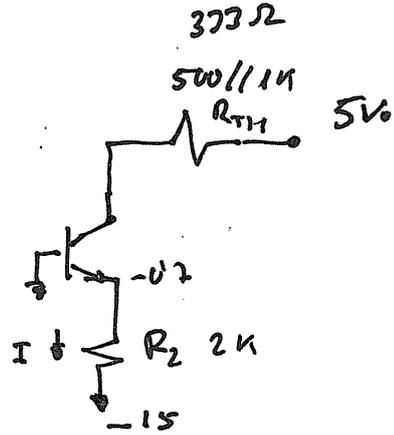
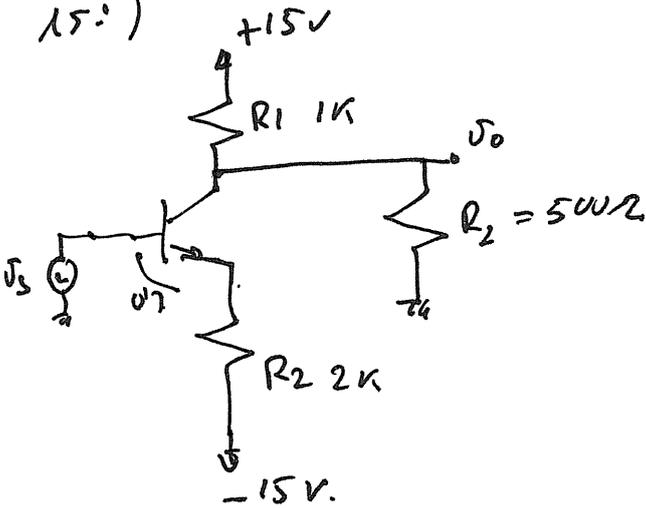
TRANSISTOR NPN.

$$\left. \begin{aligned} V_{BE} = V_d > 0 & \quad V. BE \text{ DIRECTA} \\ V_{BC} = 0 < V_f & \quad V. BC \text{ INVERSA} \end{aligned} \right\} = R. A. M$$



$$\left. \begin{aligned} V_{BE} = V_d > 0 & \quad V. BE \text{ DIRECTA} \\ V_{BC} = V_d & \quad V. BC \text{ DIRECTA} \end{aligned} \right\} = R. SATURADA$$

15:)



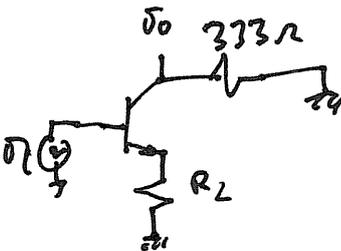
$$I_{R2} = \frac{-0.7 + 15}{2k} = 7.15 \text{ mA}$$

$$V_C = 5 - 7.15 \cdot 10^{-3} \cdot 373 = 2.62 \text{ V}$$

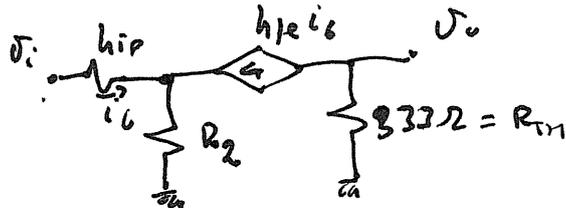
$$V_E = -0.7$$

$$V_C - V_E = 2.62 - (-0.7) = \underline{\underline{3.32 \text{ V}}}$$

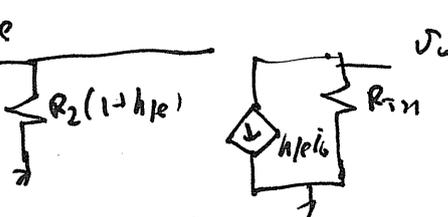
CIRCUITO EQUIVALENTE EN ACTIVA:



CIRCUITO INCREMENTAL EN EQUIVALENTE:



$$V_0 = -R_{TH} h_{ie} i_b = -\frac{R_{TH} \cdot h_{ie}}{h_{ie} + R_2(1+h_{ie})} V_i$$



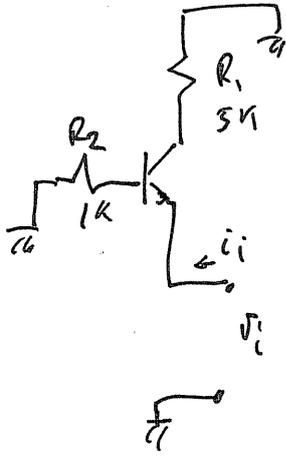
$$\frac{V_0}{V_i} = -\frac{R_{TH} h_{ie}}{h_{ie} + R_2(1+h_{ie})} \approx -\frac{R_{TH}}{R_2}$$

$$h_{ie} = \frac{V_T}{I_{CQ}} = \beta_F$$

$$h_{ie} = \frac{25 \text{ mV}}{7.15 \text{ mA}} \approx 200$$

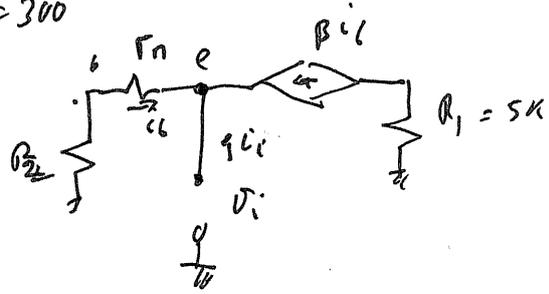
$$h_{ie} \approx 700 \Omega$$

Ej. 14.



$I_{CQ} = 1 \text{ mA}$      $r_o = \infty$

$\beta_F = 300$



$$+V_i \left( \frac{1}{r_{\pi} + R_2} \right) - \beta i_b = i_c =$$

$$i_c = - \frac{V_i}{r_{\pi} + R_2}$$

$$+V_i \left( \frac{1}{r_{\pi} + R_2} \right) + \frac{\beta}{r_{\pi} + R_2} V_i - i_c = 0$$

$$+V_i \left[ \frac{1}{r_{\pi} + R_2} + \frac{1}{\frac{r_{\pi} + R_2}{\beta}} \right] = i_c$$

$$r_{\pi} = \frac{V_T}{I_{CQ}} \beta =$$

$$\frac{26 \text{ mV} \cdot 300}{1 \text{ mA}} = 7.8 \text{ k}$$

$$\frac{V_i}{i_c} = \frac{1}{\frac{1}{r_{\pi} + R_2} + \frac{1}{\frac{r_{\pi} + R_2}{\beta}}} = (r_{\pi} + R_2) \parallel \frac{r_{\pi} + R_2}{\beta} \approx$$

$$\frac{r_{\pi} + R_2}{\beta} = \frac{7.8 \text{ k} + 1 \text{ k}}{300} = 29.13 \text{ } \Omega$$

